

156 1. $\frac{x\sqrt{x}}{\ln(x)} = \sqrt{x} \frac{x}{\ln(x)} = \sqrt{x} \frac{1}{\frac{\ln(x)}{x}}$.

On a $\lim_{x \rightarrow +\infty} \frac{\ln(x)}{x} = 0^+$ donc $\lim_{x \rightarrow +\infty} \frac{1}{\frac{\ln(x)}{x}} = +\infty$.

De plus $\lim_{x \rightarrow +\infty} \sqrt{x} = +\infty$.

Ainsi, $\lim_{x \rightarrow +\infty} \frac{x\sqrt{x}}{\ln(x)} = \lim_{x \rightarrow +\infty} \sqrt{x} \times \frac{1}{\frac{\ln(x)}{x}} = +\infty$.

2. $2x^3 - 1 - \ln(x) = x^3 \left(2 - \frac{1}{x^3} - \frac{\ln(x)}{x^3} \right)$.

On a $\lim_{x \rightarrow +\infty} \frac{\ln(x)}{x^3} = 0$ et $\lim_{x \rightarrow +\infty} \frac{1}{x^3} = 0$ donc $\lim_{x \rightarrow +\infty} 2 - \frac{1}{x^3} - \frac{\ln(x)}{x^3} = 2$.

On a aussi $\lim_{x \rightarrow +\infty} x^3 = +\infty$.

Ainsi, $\lim_{x \rightarrow +\infty} 2x^3 - 1 - \ln(x) = \lim_{x \rightarrow +\infty} x^3 \times \left(2 - \frac{1}{x^3} - \frac{\ln(x)}{x^3} \right) = +\infty$.